2001 - 2002

AMERICAN COMPUTER SCIENCE LEAGUE

Contest #3

Senior Division Programming Problem

PALINDROME

PROBLEM: A positive integer is said to be a palindrome with respect to base b, if its representation in base b reads the same from left to right as from right to left. Palindromes are formed as follows:

Given a number, reverse its digits and add the resulting number to the original number. If the result isn't a palindrome, repeat the process. For example, start with 87 base 10. Applying this process, we obtain:

87 + 78 = 165 165 + 561 = 726 726 + 627 = 13531353 + 3531 = 4884, a palindrome

Whether all numbers eventually become palindromes under this process is unproved, but all base 10 numbers less than 10,000 have been tested. Every one becomes a palindrome in a relatively small number of steps (of the 900 3-digit numbers, 90 are palindromes to start with and 735 of the remainder take fewer than 5 reversals and additions to yield a palindrome). Except, that is, for 196. Although no proof exists that it will not produce a palindrome, this number has been carried through to produce a 2 million-digit number without producing a palindrome.

INPUT: 5 sets of data. Each set will consist of a positive integer and its base. Bases will be in the range 10 - 16.

OUTPUT: Print the palindrome produced. If no palindrome is produced after 10 additions, print the word "none" and the last sum.

SAMPLE DATA

- 1. D4D
- 2. 9B4B9
- 3. NONE, 18211171

SAMPLE OUTPUT

- 1. A23, 16 2. A345, 12
- 3. 196, 10

AMERICAN COMPUTER SCIENCE LEAGUE

2001 - 2002

Senior Division Test Data

PALINDROME

Test Data

- 1. 6A, 16
- 2. 5896, 13
- 3. 8769, 15
- 4. 46894, 10
- 5. AAB4, 12

Test Output

- 1. 121
- 2. BB8AA8BB
- 3. 45522554
- 4. NONE, 1317544822
- 5. 3A88A3

-

Contest #3